

$x = ()$	$y = ()$	$x = ()$	$y = ()$
2.5	2.5	2.5	2.5
2.2	3.25	2.40625	2.3125
2.36364	7.5625	2.35828	2.302802
2.26923	54.1914	2.33288	2.302776
2.32203	2933.71	2.31920	2.302776
2.29197	8606642.63	2.31176	2.302776
2.30892	741	2.30770	2.302776

The function $f(x)$, $g(x)$ converges to the solution while $h(x)$ diverges

The function $g(x)$ is converges to the solution if $|g'(x)| < 1$

Example $g(x) = 1 + x^{-2}$, $x = -2.05$

$$g(x) = 1 + x^{-2}, \quad x = -2.05$$

$$g(x) = 1 + x^{-2}, \quad x = -2.05$$

$$g(x) = 1 + x^{-2}, \quad x = -2.100625$$

$$g(x) = 1 + x^{-2}, \quad x = -2.0378135$$

$$g(x) = 1 + x^{-2}, \quad x = -2.41794441$$

The sequence does not converge to $x = -2$

$$g(x) = 1 + x^{-2}, \quad x = 1.6$$

$$1$$

$$= 1.6$$

$$= 1.96$$

$$= 1.9996$$

$$= 1.9999996$$

The sequence converge to $x = -2$

Aitken formula for accelerating convergence

$$= - , n = 0, 1, 2, 3, \dots$$

Example Find the root of $f(x) = -x - 3$ in $[2,3]$, $= 2.5$

$$g(x) =$$

$$= 2.5$$

$$= g() = 2.40625$$

$$= g() = 2.35828$$

$$= - = 2.3080157$$

$$= g() = 2.3288$$

$$= - = 2.3042979$$

Consider the following system

$$(x,y) = 0 , (x,y) = 0$$

1) Fixed point iterative theorem

$$= ()$$

$$= () , , n = 0 , 1 , 2 , \dots$$

The condition for converges is

$$L = \max\{+ , 1$$

Stopping condition and

Example

$$(x,y) = + -4 , (x,y) = y - , = (1,1)$$

$$X = = (x,y)$$

$$Y = = (x,y)$$

$$L = \max\{+ , \} = \max\{+ , \}$$

$$L = \max\{+ , \} = \max\{ , \} = 1$$

$$= () = 1$$

$$= () =$$

$$= () =$$

$$= () =$$